# Valence Stability and Madelung Self-Site Potential of Alliovalent Ions in Various Oxide Lattices

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#### "Stabilization of High - Valence States of Ions at B - site of Perovskite Structure ABO<sub>2</sub>: Electrostatic Potential in Perovskite Structure"

By

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#### Synopsis

The perovskite-type compounds,  $A^{2+}B^{4+}O_3$  (A = Ba, Sr, B = Ce, Pr, Tb), were synthesized by the reaction between ACO<sub>3</sub> or AO<sub>2</sub> and B-Oxides.  $A^{2+}B^{4+}O_3$  were stable under the conditions where B<sup>4+</sup>O<sub>3</sub> with fluorite structures were no longer stable. This fact was explained by the contribution of lattice energy. That is, the lattice self-potential of B-site in perovskite structure is stronger than that in fluorite structure. It was demonstrated that the stability of valence states of ions was related to the lattice self potentials at those ion-sites in crystal lattices.

From the comparison of the potentials calculated for every sites in several crystal structures, perovskite, corundum, rutile, fluorite etc., it was shown that a certain ion had the maximum potential at B-site of perovskite structures. It was concluded that high valence states were stabilized at B-sites of perovskites which had the strong potentials, even in the cases of other ions, Ni<sup>3+</sup>, Co<sup>3+</sup>, Fe<sup>4+</sup>, Mn<sup>4+</sup>, etc.

They were also explained by the self-potentials that perovskites would have the point defects at A-sites or oxygen sites, and that  $A^{**}B^{**}O_s$  type perovskites would not exist.

This was refered By R.Roy in his Orton lecture at Am.Ceram.Soc. 1976,Bull.Am. Ceram.Soc.(1976)



 $CeO_2+(1/2)V_2O_5 \xrightarrow{} CeVO_4+(1/4)O_2$  $Ce^{3+}[V^{5+}O_4]$ 

Cerium was reduced in air.

**Zircon structure** 

This compd does not decompose (oxidize) even under  $Po_2 > 10^3$  atm.

TG-DTA curves for the reaction In air (Po<sub>2</sub>=0.21 atm) (Yoshimura '69)



The relationship between the oxygen partial pressure and the composition of Cerium oxide. (a) 1000, 1100, and 1200° C; 8b) 1153, 1200, 1249, 1310, and 1130° C Kitayama, et al. ('85) J. Solid State Chem.



 $VO - V_2O_5$  phase diagram

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#### A New Monoclinic Phase of Cerium Orthovanadate (CeVO<sub>4</sub>)

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A new monoclinic phase of cerium orthovanadate,  $CeVO_4(H)$ , was found during the course of oxidation of pseudo-perovskite  $CeVO_3$  below 400°C. It has been confirmed to crystallize in the huttonite-type structure ( $C_m^* - P2_3/v$ ), that of  $LaVO_4$ . The lattice parameters were determined to be:

 $a_b = 6.98 \text{\AA}, \ b_s = 7.22 \text{\AA}, \ c_s = 6.76 \text{\AA}, \ \beta = 105'02', \ V = 328 \text{\AA}^s \text{ and } Z = 4.$ 

This phase was metastable, and exothermally transformed into a known stable CeVO<sub>4</sub> (tetragonal zircon-type,  $D_{ab}^{a}$ - $P4_{1}$ /and) above 400°C, releasing a small amount of oxygen. From magnetic, chemical and thermogravimetric analyses, the valences of cerium ion and vanadium ion in CeVO<sub>4</sub>-(H) seem to be tripositive and pentapositive respectively, but V<sup>4+</sup> ion is mixed in zircon-type  $GeVO_4$ ;  $GeVO_4(Z)$ .

#### **Recent Papers on Valence Stability of Rare Earth Ions**

- 1) "Understanding of the Valency of Rare Earths from Firstprinciple Theory," P. Strange, A. Svane, W. M. Temmermann, Z. Szotek, and H Winter, Nature 399 (24 June 1999) 756-758
- 2) "Valence Stability of Lanthanide Ions in Inorganic Compounds," P. Dorenbos, Chem. Mater. 17 (2005) 6452-6456
- 3) "The Eu3+ Charge Transfer Energy and the Relation with the Band Gap of Compounds," P. Dorenbos, J. Lumin, 111 (2005) 89-104
- 4) "Stability of Rare Earth Oxychloride Phases: Bond Valence Study," J. Hölsä, M. Lahtinen, M. Lastusaari, J. Valkonen, and J. Vijanen, J. Solid State Chem., 165 (2002) 48-55
- 5) "Critical Materials Problems in Fuel Cells: SOFC'S," H. Yokokawa, Oxford, April 02, 2007



Figure 4.  $E_{\rm Ff}$  for Eu<sup>2+</sup> in oxide, chloride, and sulfide compounds. The solid triangle symbols pertain to Eu on Ba<sup>2+</sup>, Sr<sup>2+</sup>, Ca<sup>2+</sup>, or Mg<sup>2+</sup> sites and in addition to Eu in RbCl and KCl. The other data are the same data as in Figure 3 and pertain to Eu in trivalent rare earth oxide compounds. The box around date with  $E_{\rm VC}$  > 8 eV and  $E_{\rm Ff}$  < 0.7 eV contains alkaline carth compounds in which Eu<sup>2+</sup> can be obtained even under oxidizing conditions. P. Dorenbos, Chem. Mater. (2005) <u>17</u>, 6452



H. Yokokawa (AIST, Japan), Apr. 2007



Enthalpy Diagram for the reduction of rare earth (A) Manganates; T. Nakamura (1985) AMnO<sub>3</sub>(s) =  $\frac{1}{2} A_2O_3(s) + MnO(s) + \frac{1}{4} O_2(g)$ 



Energy Diagram for the Reaction:  $MO_{\frac{3}{2}}(s) + \frac{1}{4}O_2(g) \rightarrow MO_2(s)$  [  $\Delta G^{\circ}_{r}$ ] U: Lattice energy, D: Dissociation energy, A: Electron affinity  $H_{f}^{\circ}$ : Standard formation enthalpy,  $I_4$ : 4th Ionization energy  $MO_{3/2}$  +  $1/2O_2$  =  $MO_2$  ···  $\Delta G$ 



Lattice energy (U) is also given by

$$U = Ne^2 \sum_j \frac{q_j p_j \phi_j}{2k}$$

N: Avogadro No. sublattice qj: Valency of j-ion *(j*: Lattice-site potential of j-ion pj: Occurence of j-ion in the unit cell k: Molecular No. in the unit cell  $\boldsymbol{U} = -331.98 \left(\frac{\boldsymbol{M}_a}{\boldsymbol{a}}\right)$ [kcal/mol] for  $\phi$  [A<sup>-1</sup>]  $M_a = -a \sum_{j} \frac{q_j p_j \phi_j}{2k}$ 

## Madelung Lattice Site Potentials in Europium Containing Oxide

Compound		structure	Lattice site potential		
			$\phi_{Eu}$	φ <sub>M</sub>	φ <sub>O</sub>
Eu <sup>2+</sup>	EuO	NaCl	-1.359		1.359
	EuTiO <sub>3</sub>	Perovskite	-1.380	-3.171	1.653
	Eu <sub>3</sub> O <sub>4</sub>	Eu <sub>3</sub> O <sub>4</sub>	-1.377	-2.076/-2.088	1.423~1.457
Eu <sup>3+</sup>	Eu <sub>2</sub> O <sub>3</sub>	B-type	-2.081 <b>~</b> -2.107		1.432~1.507
	EuFeO <sub>3</sub>	Perovskite	-2.051	-2.500	1.576/1.602
	EuMnO <sub>3</sub>	Perovskite	-2.055	-2.495	1.574/1.633
	EuScO <sub>3</sub>	Perovskite	-2.038	-2.382	1.543/1.557
	Eu <sub>2</sub> Ti <sub>2</sub> O <sub>7</sub>	Pyrochlore	-2.167	-3.100	1.523/1.640
	EuPO <sub>4</sub>	Zircon	-2.116	-4.160	1.882~1.970

## Madelung Lattice Site Potentials in Cerium Containing Oxide

Compound		structure	Lattice site potential		
			$\phi_{Ce}$	φ <sub>M</sub>	φ <sub>O</sub>
Ce <sup>3+</sup>	Ce <sub>2</sub> O <sub>3</sub>	A-type	-2.036		1.400/1.405
	CeAlO <sub>3</sub>	Perovskite	-1.965	-2.738	1.578/1.582
	CeCrO <sub>3</sub>	Perovskite	-1.908	-2.659	1.535
	CeGaO <sub>3</sub>	Perovskite	-1.915	-2.669	1.540/1.547
	CeVO <sub>4</sub>	Zircon	-2.103	-3.697	1.803
	CeTaO <sub>4</sub>	d-Sheelite	-2.136	-3.595	1.52~1.79
	LiCeO <sub>2</sub>	NaFeO <sub>2</sub>	-1.962	-1.080	1.438/1.474
	CeTa <sub>3</sub> O <sub>9</sub>	Layered Perovskite	-2.126	-3.646/-3.660	1.679~1.808
Ce4+	CeO <sub>2</sub>	Fluorite	-2.797		1.504
	BaCeO <sub>3</sub>	Perovskite	-2.816	-1.226	1.468
	SrCeO <sub>3</sub>	Perovskite	-2.893	-1.256	1.503





(1)  $|\phi_B| > |\phi_A|$ (2)  $\phi_O$  decrease with valency-pair from 0-6 to 3-3. (3) Ma decrease with valency-pair from 0-6 to 3-3.



 $\frac{1/2La_2O_3+1/2Al_2O_3}{\Delta U=-35Kcal/mol} \rightarrow LaAlO_3$ 

Site self potential change for the Gain formation of LaMO<sub>3</sub> from La<sub>2</sub>O<sub>3</sub>+M<sub>2</sub>O<sub>3</sub>

 $\Phi$  for Co<sub>2</sub>O<sub>3</sub> and Ni<sub>2</sub>O<sub>3</sub> in High-Spin & Low-Spin states are estimeated from ionic radii.

Co<sup>3+</sup>, Ni<sup>3+</sup> etc. stabilized by strong  $\Phi_{\rm M}$ 

B-ion has a 6-coordination in LaMO<sub>3</sub> as well as in M<sub>2</sub>O<sub>3</sub> (MO<sub>2</sub>, MO, .....)



Change of Lattice Site Potentials of Every Site in the Reacton  $SrO + MO_2 = SrMO_3$ 

# Lattice energy change in the formation of EuTiO<sub>3</sub>

a)  $EuO + TiO_2 = Eu^{2+}Ti^{4+}O_3 + Q$ (-902) + (-3256) = (-4210) + (-52) (-4158)

b)  $(1/2)Eu_2O_3+(1/2)Ti_2O_3=Eu^{3+}Ti^{3+}O_3+Q$ (1/2)(-3570) + (1/2)(-4031) = (-3806) + (-6)(-3800)



FIG. 5. The phase equilibia in the Ce<sub>2</sub>O<sub>3</sub>-Fe-O system at 1200°C. Numerical values in the three solid phases regions are the equilibrium oxygen partial pressure in  $-\log P_{O_2}$ . Symbols are the same as those in Table I.

#### KITAYAMA ET AL ('85)

## Summary

(1) Valence stability is different in ternary systems from binary systems.

$$X-P_{O2}$$
 - T diagramin  $RO_x$  $X-y-P_{O2}$  - T diagramin  $RM_yO_x$ 

(2) Valence stability is directly related to electrostatic lattice-site potential ( $\phi$ ),

$$U = Ne^{2}\Sigma \frac{pq\phi}{2k} \implies 331.98\Sigma \frac{pq\phi}{2k} \text{ [kcal/mol] for } \phi \text{ [Å]}$$

(3) for example:

 $\varphi\approx$  1.36-1.38 for Eu^{2+},  $\varphi\approx$  2.04-2.17 for Eu^{3+}

 $\varphi\approx$  1.8-2.1 for Ce^{3+},  $\varphi\approx$  2.8-2.9 for Ce^{4+}

- (4) In perovskite (ABO<sub>3</sub>) lattice, High valency state in B-site & difficult defect formation in B-site due to strong  $\phi_B$  potential.
- (5)  $CeO_2$  may be reduced during the reaction with  $MO_x$  when M is high valent, small ion and  $MO_x$ -rich part.

Oxysalt :  $Ce^{3+}[MO_y]_x$ 



#### **Prof. Sata**



### **Prof. Somiya**

